

University of Oxford

Keble College  
Hilary term  
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CP3: Mathematical Methods 1

## Additional homework problem

**Problem B.1.** Positive charge  $Q$  is uniformly distributed over an infinitely thin wire shaped as a ring of radius  $R$ . The ring is positioned in the  $XY$  plane and centred at  $(x, y, z) = (0, 0, 0)$ .

- a) Find the magnitude and direction of the electric field at the point  $(0, 0, h)$ , where  $h \ll R$ .
- b) Find the magnitude and direction of the electric field at the point  $(r, 0, 0)$ , where  $r \ll R$ .
- c) Is your result consistent with the divergence theorem applied to the cylinder of radius  $r$  and height  $2h$ , centered at the origin? The base of the cylinder is parallel to the  $XY$  plane.